NASA TT F-11,510

# RECENT DEVELOPMENTS IN WIND-TUNNEL MEASUREMENTS OF AERODYNAMIC DERIVATIVES

M. Scherer and J. Lopez

Translation of "Progres Realises dans les Techniques de Mesure des Derivees Aerodynamiques en Soufflerie Methode d'Oscillations Forcees"

Office National d'Etudes et de Recherches Aerospatiales, TP 389, 1967, 32 p.

	GPO PRICE \$	
	CFSTI PRICE(S) \$	
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## RECENT DEVELOPMENTS IN WIND-TUNNEL MEASUREMENTS OF AFRODYNAMIC DERIVATIVES

#### M. Scherer and J. Lopez

ABSTRACT. Some of the most important unsteady-testing devices used in wind-tunnels are presented. These devices give the complete set of derivatives, the knowledge of which is necessary to the study of flight mechanics of planes or missiles. The tests can be carried out in continuous or in intermittent wind-tunnels. Sting dynamometers and micro-accelerometers equipped with silicium strain-gages are now employed. An example is given for comparison of the wind-tunnel measurements; it deals with the measurement in flight and in wind-tunnel of the STOL-Breguet 941 in landing configuration.

#### 1. Introduction

The object of this publication is to offer a glance at the progress made at /3\* 1'O.N.E.R.A. in the measurement of aerodynamic derivatives by the method of forced oscillations since the communication made in Brussels in 1961 [1].

A preliminary remark is necessary: unsteady derivatives represent only one aspect of the information required solely for studies of flight quality. As a result, their determination in a wind-tunnel will be of interest to designers only if they are obtained easily and rapidly. On the other hand, however, a relatively broad tolerance in terms of precision will be admitted.

It is with this in mind that the O.N.E.R.A. measurement installations were created and developed; some operate with forced oscillations and others operate with free oscillations [2].

The disclosure to follow will deal strictly with the method of forced oscillations.

The principles of these methods are well known and will be brought up only to refresh the reader's memory. The considerable progress achieved in measurement techniques in recent years will be especially stressed.

The principal installations of this type now in service at O.N.E.R.A. will be presented.

Some cross-checking against flight measurement will give an idea of the validity of the wind-tunnel results.

<sup>\*</sup> Numbers in the margin indicate pagination in the foreign text.

#### 2. Notations

3.1.

The notations used are in conformity with the French standards X 02-105.

Special notations are presented:

Jetstream Mounting

- in the table in Plate 2, where the expressions for the dimensionless coefficients of the aerodynamic derivatives are given.
- in the figures in Plate 3, where the fixed reference axes and the reference axes related to the mock-up are given, as well as the symbols for the angles, the components of the resulting moment  $(L_1, M_1, N_1)$  and for the angular velocity  $(p_1, q_1, r_1)$  on the axes bound to the mock-up (Figure 1).

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#### 3. <u>Description of Principal Arrangements and Methods</u>

The mock-up is attached to the end of a dynamometric sting similar to those used for stationary measurements.

Strain gages are fastened to the forward part of the sting and assembled in combination by groups of four, each of which is a moment dynamometer.

Five dynamometers are thereby formed which yield the projected moments according to two systems of axes, specifically:

$$0_1^1 \quad x_1 \quad y_1^1 \quad z_1^1 \quad , \quad 0_1^2 \quad x_1 \quad y_1^2 \quad z_1^2 \quad ,$$

having in common the axis  $0_1^1$   $0_1^2$   $x_1$  and reduced one from the other by translation of  $0_1^1$   $0_1^2$  along the  $x_1$  axis (Figure 2).

The subscript 1 indicates that the system of axes is connected to the sting and therefore to the mock-up, and the superscript is used to differentiate them.

The component parallel to the sting is not measured. The names and symbols of the five components are indicated in the table below.

Angular elongation of the movement of the mock-up during oscillation is measured by a detector equipped with strain gages similar to those of the dynomometers (Figure 3). This detector is indicated by D in Figure 5.

#### 3.2 Setting into Motion

Constant low-amplitude oscillations ( 2°) with constant frequency

 $(1 < f \le 20 \text{ Hz})$  are fed the mock-up and the sting successively around the three axes either blended with or parallel to the axes defined above, by a simple mechanical device.

**TABLE** 

Measured	Symbol	! Reduction axis of )
Ro11	$^{ m L}$ 1	$\begin{array}{ccc} \vdots & & & \\ \vdots & & 0 \\ \vdots & & & 1 \end{array}$
Yaw	N <sub>1</sub> N <sub>2</sub>	$\begin{array}{cccccccccccccccccccccccccccccccccccc$
Pitch	M <sup>1</sup> M <sup>2</sup>	$\begin{array}{cccccccccccccccccccccccccccccccccccc$

The roll motion around the sting axis is generally easily obtained.

In contrast, even in Modane's large supersonic wind-tunnels, the size of the mock-ups presently being used does not in practice permit the use of oscillations around an axis passing through the representative point for the center of gravity in the aircraft or engine undergoing tests.

For measurements in supersonic or transonic wind-tunnels, this reason has resulted in the fixing of the pitch or yaw oscillation axes downstream from the mock-up.

Allowance has been made in computations for the lack of concurrence between the oscillation and measurement axes [§ 3.3].

#### 3.3 Measurement Methods

The indications for the dynamometer and position detector as a function of time are treated by harmonic analysis limited to the frequency of the motion imposed.

This method of operation has the advantage of automatically eliminating from the measurement results the parasite responses introduced by the continuous components and harmonic resulting from noises of the wind-tunnel and the mounting.

This limitation is sufficient if the responses are linear, a frequent case in practice. Two processes are used for the application of the method:

1) The first, developed and perfected 15 years ago, applies to continuous wind-tunnels. In this process, the wind-tunnel data are obtained by direct reading during the tests.

It consists of feeding the gage bridges by a sinusoidal current with constant intensity and a frequency identical to that of the motion imposed (Plate 5).

The phase for this current is repeatedly adjusted, first in coincidence with the motion and then squared. Constant-current galvanometers, the same as those used for stationary measurement and plugged into the measurement diagonals for the bridges yield respectively:

- After the first adjustment, the amplitudes for the moment components  $R(M_1)$  etc... in phase with the motion and the amplitude of the latter  $R(\Theta_1)$  [or  $R(\psi_1)$  or  $R(\phi_1)$ ].
- Following the second adjustment, the components of the moment J (M $_1$ ) etc... in quadrature with the motion. In this case the galvanometer plugged into the position detector must show a zero indication [J ( $\theta$ ) = 0], according to the definition of the square.

It is precisely in acting on the phase converter so as to cancel the galvanometer reading that the adjustment is first achieved then maintained throughout the measurement.

2) In the second process, the gages are fed a continuous current and the responses fixed in the bridge measurement diagonals are treated by harmonic analysis (Plate 6).

This may be done in two ways:

- 1 Immediately during the tests by an analogical means.
- 2 Delayed and using a magnetic recorder; in this case the harmonic analysis may be carried out with the same precision by either a numerical or analog process.

The advantage of delayed clearing is that it permits measurement of forced oscillations in intermittent wind-tunnels where the useful duration of the flow is on the order of one second.

Tests in the fine adjustment of this measurement chain were carried out in the O.N.E.R.A. intermittent wind-tunnel at Chalais-Meudon equipped with a Mach 10 tube through measurement of the pitch derivatives of a mock-up of a blunt cone [3].

This setup is presently being adapted to industrial measurement.

In each case, the data of harmonic analysis, direct or delayed, are then transformed into the dimensionless coefficients indicated in Plate 2.

These calculations, performed automatically, introduce various corrections (energy forces, non-measured support deformations, non-concurrence of oscillation and measurement axes).

The calculation programs on the IBM 704 will be the subject of another publication.

#### 4. Progress Achieved

The progress which has been achieved in the last four years has had a bearing on both improving the measurement chains and the development of the mounting installations.

#### 4.1 Measurement and Control Channels

Electronic Equipment.

Various types of equipment designed almost integrally with commercially mass-produced transistorized sets have been put into service:

- controlled feed of the electric motors which perform the oscillation motions.

The rotation speed is maintained constant to better than 1% in a range of values which are continuously adjustable from 2 to 50 rps. The error signal is given by the voltage to the terminals of a tachometer generator which is compared to an adjustable reference voltage.

- frequency meters, which are composed basically of an electric pulse generator and a counter.

The pulses are produced by the interception of a luminous ray aimed at a photoelectric cell by crenels which are mounted around the circumference of a disk turning with the same speed as the balance motor.

- a sinusoidal current generator with constant intensity and adjustable phase. It is composed of a constant-modulus symmetrical phase converter which was developed at O.N.E.R.A. and several continuous commercially produced transistorized amplifiers. The intensity of the current is maintained constant at better than 1% deviation, no matter what the phase adjustment;

the current which is delivered makes it possible to feed the 10 gage bridges which handle 120 ohms at 16 volts, from peak to peak. The phase adjustment threshold is on the order of 1 milliradian.

The frequency level runs from 2 Hz to 100 Hz. The current direction can be inverted and the phase changed manually and quite rapidly.

- The silicium semi-conductor gages which are presently being put into service and which are 60 times more sensitive than resistance wire gages have made it possible to make some substantial progress with respect to the elements linked to the table mountings. The following example gives an idea of the use of these gages:

It has been possible to increase the sensitivity of the roll dynamometer by seven times and its rigidity by five times through replacing the resistance wire gages which were attached to a support with a cross-shaped section area by semi-conductor gages attached to a support with a rectangular section which encompasses the former area (Figure 4).

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The interactions are more important with the gages attached to the sting axis at 45°; however, they are not restrictive since they can be determined quite precisely.

It is to be hoped that in the future these interactions will be diminished through improving the technique of mounting the gages.

Like the dynamometers, the position detectors have been equipped with silicium gages.

- On the other hand, due to the small size of these gages as can be seen from the dimensions:

length 4 mm, width 1 mm, thickness 20 microns, the Department of Physics at O.N.E.R.A. has been able to perfect accelerometers with dimensions which are small enough to permit their being installed inside the mock-ups  $(4 \times 2 \times 15 \text{ mm})$ .

The measurement threshold is  $2.5 \times 10^{-3}$ g and their natural frequency is greater than one kilocycle.

An example of the installation for these accelerometers is given in Figure 11 and  $\S$  4.3.3.1.

#### 4.2 A Comment on the Joints

The use of flexible joints as are currently used in the automobile industry has been adopted for all the balances. As a reminder, it should be pointed out here that they consist of two concentric steel rings (Figure 5) inter-connected by a rubber ring. This piece of equipment, which permits easy correction of alignment errors, is of special interest in damping the

shocks at the peak of the test when the motion amplitude reaches its maximum values.

#### 4.3 Development of the Installations

#### 4.3.1 Installation at Chalais-Meudon

At O.N.E.R.A.'s Aerodynamic Research Center at Chalais-Meudon, the measurement of derivatives is conducted along industrial lines in all the wind-tunnels.

It was pointed out earlier (§ 3.3) how this method was extended to cover intermittent wind-tunnels.

The test control organs and the measurement instruments are combined in a measurement station (Plate 8) which is linked up to the wind-tunnels and the laboratory where the mountings are given final adjustment; the communication lines with the transonic wind-tunnel  $S_3$  are up to 800 m long. It was considered of interest to point out this detail due to the very low values of the measurement currents (on the order of  $10^{-9}$  A). This arrangement offers great flexibility in the manner in which the installations function and eliminates the need to move the measurement and control instruments or duplicate them.

#### 4.3.1.1 Example of Mounting on the Subsonic Table

Only one example is given here for the mountings used in recent years. It can be installed either in the large subsonic wind-tunnel  $S_1$  or in the  $S_2$  wind-tunnel. It permits the mock-up to undergo successively oscillations of pitch (Figure 5), yaw (Figures 6 and 7) and roll (Figure 8 and 9).

Plate 12 gives its basic characteristics.

The results obtained with this installation can be compared to flight measurements. Such a comparison is made below in § 5.

# 4.3.3 The O.N.E.R.A. Transonic and Supersonic S<sub>2</sub> Wind-Tunnel Installations at Modane

Following the adjustments made on the installation at the small wind-tunnels at Chalais-Meudon, two mountings were built to equip this wind-tunnel [4], which has a rectangular experimental stream channel which is  $1.87 \times 1.75$  m and in which the generating pressure  $p_{\hat{\mathbf{i}}}$  and the Mach number M can be controlled continuously at the respective intervals of:

$$0.2 \le p_i \le 2 \text{ bars}$$
 
$$0.2 \le M \le 1.3 \qquad \text{and} \qquad 1.5 \le M \le 3.2$$

<u>/9</u>

The first mounting sends roll oscillations to the mock-up and the second instills pitch and yaw oscillations.

# 4.3.3.1 The Diagram for the Roll Balance is given in Figure 8, and its Characteristics are given in Plate 15

Figure 11 shows a view of the dynamometric portion of the sting. This figure shows the two accelerometer pick-ups which permit determination of the parasitic transverse motion of the mock-up resulting from the dynamic deformation of the sting.

Measurement of the direct derivative of the roll moment with respect to the angular velocity  $\mathbf{p}_1$ , as represented by the coefficient  $\mathbf{C}_{j}$ , in general presents no particular difficulty. In fact, the value of the total roll moment, including the mass and aerodynamic effects, does not exceed ten times that of the phase moment with  $\mathbf{p}_1$ , a condition which still permits measurement of  $\mathbf{C}_{j}$  with an approximation on the order of 10%.

In contrast, determining the coefficient  $\mathbf{C}_{np_1}$ , which characterizes the crossed derivative of the yaw moment with respect to  $\mathbf{p}_1$ , demands special precaution.

First, the absolute value of this coefficient is low, in general not exceeding one tenth that of  $\mathbf{C}_{\mathbf{I}}$  .

In addition, the yaw moments introduced by the mass and aerodynamic connections cause deformations in the sting which in turn result in other yaw moments. Experience has shown that these moments have components which are in phase with  $\mathbf{p}_1$  and which, beyond a certain frequency, substantially exceed the value to be measured.

Theoretical analysis of the phenomenon has shown that the value of the test frequency need simply be held below a specific limit in order for the correction terms to be negligible.

This conclusion has been confirmed through measurements carried out in the supersonic section of the wind-tunnel during testing of the installation's performance with a mock-up of the CONCORDE which was normally used for steady measurements (Figure 12).

#### 4.3.3.2 The Diagram for the Pitch-Yaw Balance is Given in Figure 13

A linear accelerometer of the same type as that used on the roll balance is installed to the right of the dynamometric portion of the sting. It is

not indicated in the diagram.

The indications shown by this instrument are taken as the phase origin by the quadrature adjustments discussed in § 3.3 above.

In fact, in the special case of this balance, structural damping of the section of the sting which is not setup could at higher frequencies introduce non-negligible phase displacement between the motion of a mock-up and the signal from the position detector.

#### 5. Comparison with Flight Measurements

Measurements around the three axes have been made on the mounting described in § 4.3.1.1 in the  $\rm S_1$  wind-tunnel, using a motor-driven mock-up of the BREGUET 941 short takeoff and landing aircraft on the scale of 1/7 (Figure 14).

The mass of this mock-up is 60 kg, and its span and length are slightly over 3 meters. It is equipped with four propellers which are 0.6 m in diameter, turning at 2750 rpm and driven by an electric motor installed within the fuselage and a flexible drive similar to that used in the aircraft.

In order to satisfy the laws of mechanical similarity, the operation of the propellers demand low flow velocities within the interval:

$$10 \le V \le 15 \text{ m/s}$$
.

However, the dynamometers have been shown to be sufficiently sensitive and precise measurements have been achieved in spite of this limitation.

Flight tests have been made on this aircraft with the joint cooperation of NASA and the BREGUET company.

Incidentally, the BREGUET company has simulated these tests on an analog computer, adjusting the posted aerodynamic derivatives through success adjustment in order to obtain the best comparison against flight data.

This comparison is made here on the following parameters:

- 1) Dutch roll.
- 2) Maximum responses of angular velocities for yaw  $M_1$ , roll  $p_1$  and sideslip angle j, to impetus to the rudder.
- 3) Maximum response of angular velocity of roll  $\mathbf{p}_1$  to impetus transmitted to the ailerons.

The values resulting from this study are compared to those measured in

the wind-tunnel (Plate 19). Comparison shows that the values of the measured derivatives in the wind-tunnel are in close agreement with the mean values of the derivatives read out on the computer, with the exception of the crossed roll derivatives  $c_1$  and  $c_1$ .

#### 6. Conclusion

In conclusion, it is possible at this point to furnish designers most of the aerodynamic derivatives necessary for calculation of flight mechanics, with only a slight delay and with the measurements being of a commercial nature.

Study of these derivatives with respect to acceleration has just gotten underway at O.N.E.R.A. and was patterned after the setup used at the CORNELL Laboratory in the U.S.A., although the results obtained are still too modest to be presented here.

Thus, we are beginning to obtain encouraging comparisons between flight results on aircraft studied by the unsteady methods in wind-tunnels.

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Standard or ref- erence trihedral	F O	RCES		
erence trihedral s $Gx_1$ , $y_1$ , $z_1$ is fastened to the	Longitudinal force	Transv <u>erse</u> force	Normal force	
moving body.		$-R_{y4} = \frac{\rho}{2} V^2 S C_{y4}$		
Forces and moments	- N <sub>X1</sub> - 2 · 30 ×1	1 y1 2 5 y1	2 3C24	
Dimensionless coefficients	$C_{x1} = -\frac{R_{x1}}{\frac{f}{2} V^2 5}$	$C_{y4} = -\frac{R_{y4}}{\frac{r}{2}V^25}$	$C_{z4} = -\frac{R_{z4}}{\frac{\rho}{2}V^25}$	
Velocities	Translation velo	cities of center	of gravity	
verocities	u,	V <sub>4</sub>	W <sub>1</sub>	
		DIMENSIONLESS CC	DEFFICIENTS	
Functions	R <sub>x4</sub>	R <sub>y4</sub>	R <sub>z4</sub> Normal force	
Variables	Longitudinal force	Transverse force		
Angle of incidence	$C_{x \downarrow 1} = -\frac{1}{\frac{\rho}{Z} V^{2} 5} \frac{\partial R_{x4}}{\partial i}$	•	$C_{zi1} = -\frac{1}{\frac{\rho}{2}v^25} \frac{\partial R_{zi}}{\partial i}$	
3	$C_{xj4} = -\frac{4}{\frac{\rho}{2}V^25} \frac{\partial R_{xx}}{\partial j}$	$C := \frac{1}{\sqrt{3R_{y_4}}}$		
Side-slip angle	<b>ろく</b>	-yj1 + 2V2S 01		
Aileron extension angle	$C_{x\alpha 4} = -\frac{4}{\frac{\rho}{2}V^2 5} \frac{\partial R_x}{\partial \alpha_4}$	$C_{y\alpha 1} = -\frac{1}{\frac{\rho}{2}V^{2}5} \frac{\partial R_{y4}}{\partial \alpha_{4}}$		
β, Angle of elevator extension	$C_{x\beta1} = -\frac{1}{\frac{P}{2}V^2S} \frac{\partial R_{xA}}{\partial \beta_A}$		$C_{z\beta 1} = -\frac{1}{\frac{p}{2}V^2S} \frac{\partial R_{z4}}{\partial \beta_4}$	
t e	$C_{x}S_{4} = -\frac{4}{\frac{P}{2}V^{2}S} \frac{\Im R_{xx}}{\partial S_{4}}$	i		
<b>P4</b> Roll angular velocity		$C_{yp4} = -\frac{1}{\frac{p}{2} v^2 s} \frac{\partial R_{yi}}{\partial p_4 \frac{7}{y}}$	Á	
. <b>q.</b> Pitch angular velocity			$C_{zq1} = -\frac{1}{\frac{p}{2} v^{2} 5} \frac{\partial R_{z_1}}{\partial q_1 \frac{p}{v}}$	
Yaw angular velocity	Contraction of the State of the State of State o	$C_{yr1} = -\frac{1}{\frac{\rho}{2}v^25} \frac{\partial R_{yA}}{\partial r_1 \frac{\rho}{y}}$	Livery can be take the little of the second	

The area of the second							
MOMENTS							
Ro11	Pitch	Yaw					
$L_4 = \frac{\rho}{2} V^2 S \ell C_{l_4}$	$M_4 = \frac{P}{2} V^2 5 \ell C_{m4}$	$N_4 = \frac{\rho}{2} V^2 52 C_{\text{max}}$					
$C_{14} = \frac{L_4}{\frac{P}{2} V^2 5 \ell}$	$C_{m4} = \frac{M_4}{\frac{C}{2} + M_4 C_2}$	$C_{n_1} = \frac{N_1}{\frac{\rho}{2} V^2 5 \ell}$					
	Angular velocitie	es					
P4 .	q4 -	r <sub>t</sub>					
OF AERODYNAMI	IC DERIVATIVES						
Le	M4	N <sub>4</sub>					
Roll moment	Pitch moment	Yaw moment					
	$C_{mi1} = \frac{1}{\frac{\rho}{2} \gamma^2 5 \ell} \frac{\partial M_1}{\partial \lambda}$						
$C_{1j4} = \frac{1}{\frac{p}{2}V^2SL} \frac{\partial L_4}{\partial \dot{s}}$		$C_{nj4} = \frac{4}{\frac{p}{2}V^2SL} \frac{\partial N_4}{\partial j}$					
$C_{l\alpha 4} = \frac{1}{\frac{\rho}{2} V^2 S \ell} \frac{\partial L_A}{\partial \alpha_4}$		$C_{n\alpha 1} = \frac{1}{\frac{\rho}{Z}V^25\xi} \frac{\partial N_4}{\partial \alpha_4}$					
• ,	$C_{m\beta 1} = \frac{1}{\frac{\rho}{2} V^2 SL} \frac{\partial M_4}{\partial \beta_4}$						
$C_{1\delta_{4}} = \frac{1}{\frac{\rho}{2} \gamma^{2} 5\ell} \frac{\partial L_{4}}{\partial \delta_{4}}$	-	$C_{nS4} = \frac{4}{\frac{p}{2}V^2SE} \frac{\partial N_A}{\partial S_A}$					
$C_{lp4} = \frac{4}{\frac{9}{2}\gamma^2 5\ell} \frac{\partial L_4}{\partial p_4 \frac{9}{\gamma}}$		$C_{np1} = \frac{1}{\frac{1}{2} \gamma^2 S \xi} \frac{\partial N_4}{\partial \rho_4 \frac{\eta}{\gamma}}$					
	$C_{mq4} = \frac{1}{\frac{\rho}{Z} \gamma^2 S \ell} \frac{\partial M_4}{\partial q_1 \frac{\ell}{Y}}$						
$C_{lr4} = \frac{1}{\frac{\rho}{2} \gamma^2 S \ell} \frac{\partial L_4}{\partial r_4 \frac{1}{\gamma}}$		Cnri Tvist dr. 2					

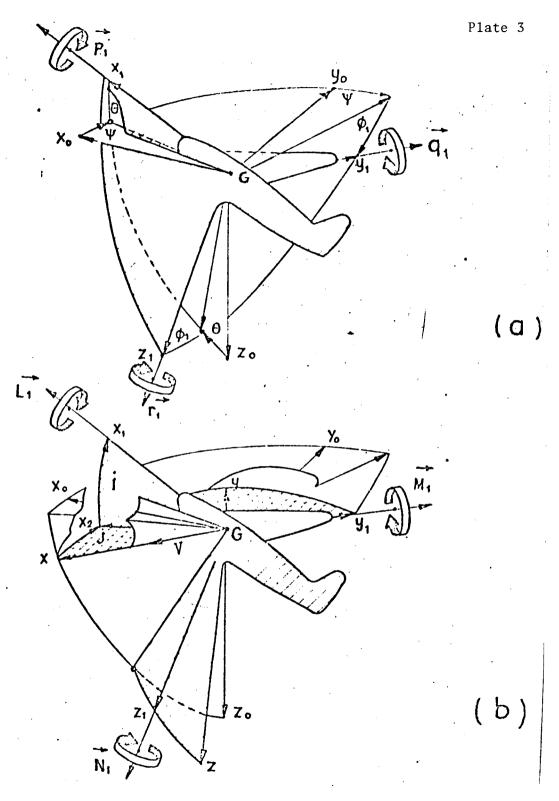


Figure 1. Coordinate Axes Defining the Position of the Aircraft in Space (a) and on Trajectory (b).

#### Caption to Figure 1

G  $x_0y_0z_0$  Galilean coordinate axis, G  $z_0$  being the vertical; G  $x_1y_1z_1$  Aircraft coordinate axis, G  $x_1z_1$  being the plane symmetry; The angles represented are positive, the curve arrows indicate the positive direction of the components of angular velocity (a) and of aerodynamic moment (b).

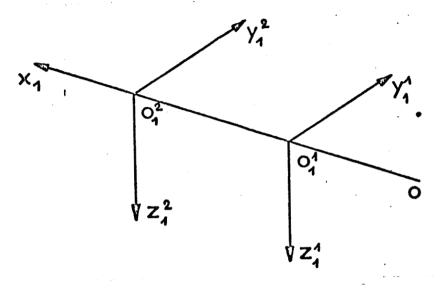


Figure 2. Sting Coordinate Axes

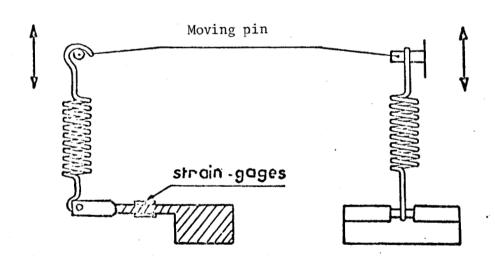
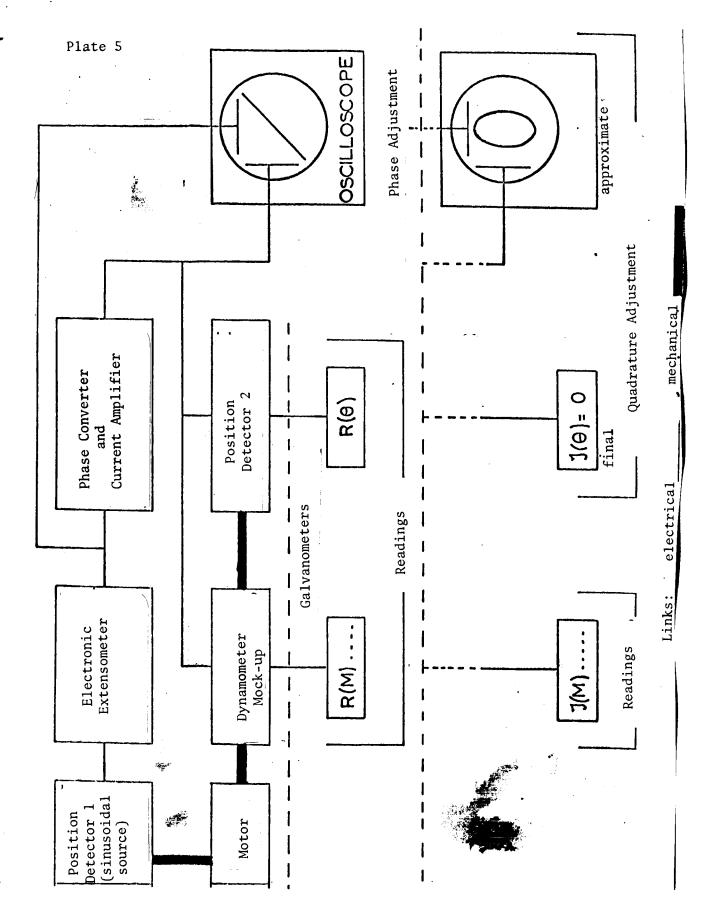
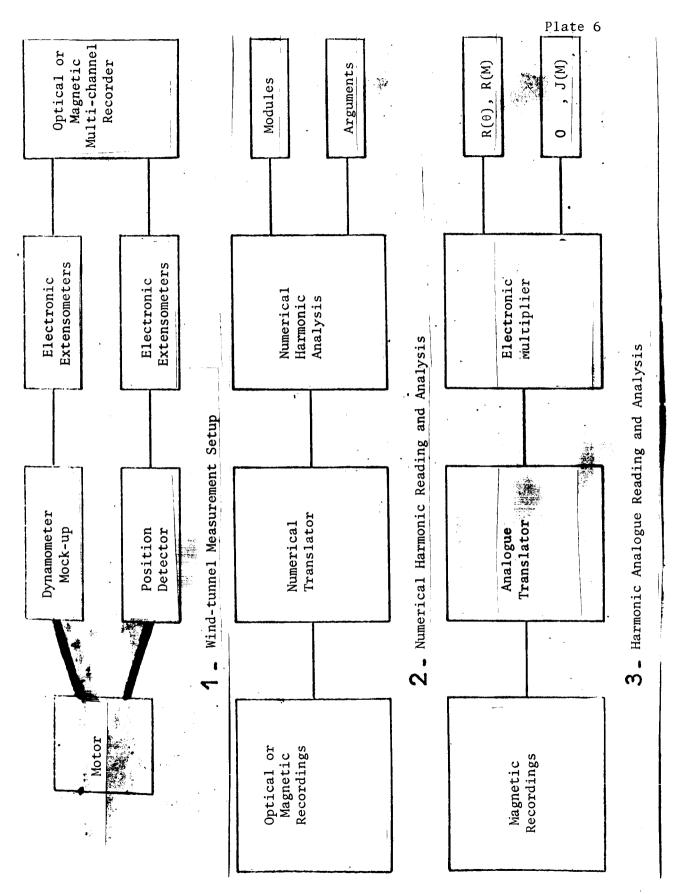
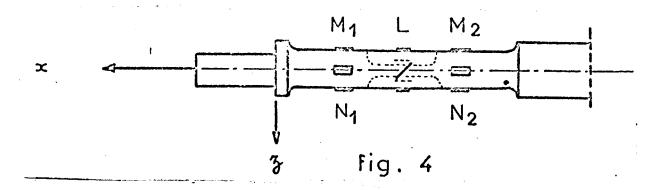


Figure 3. Position Detector

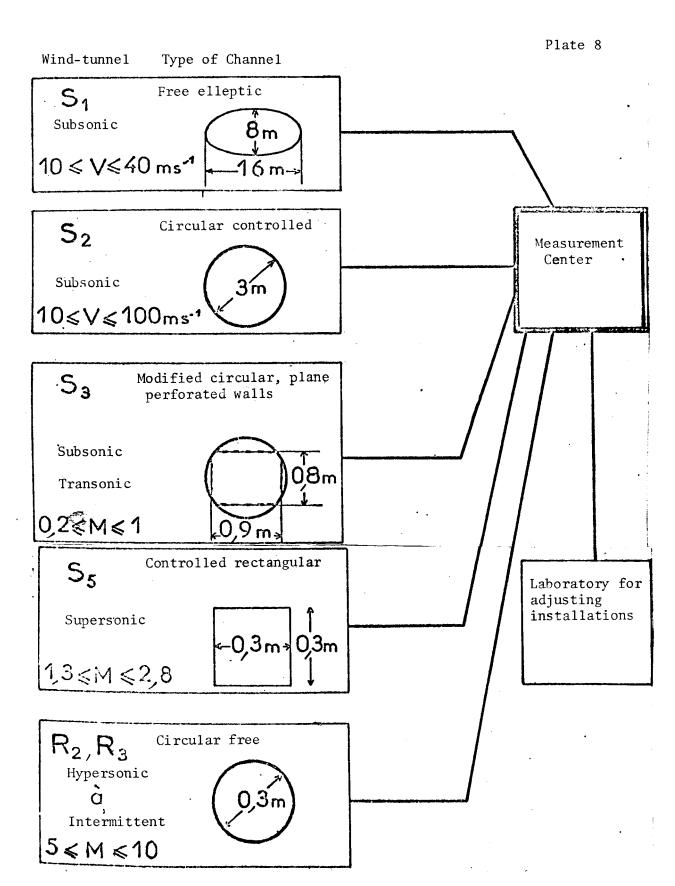


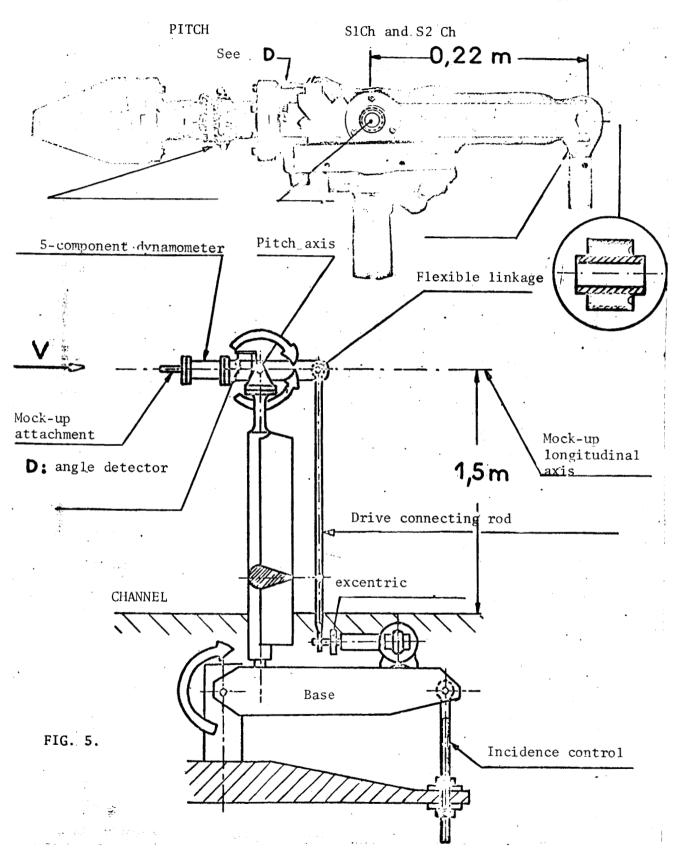


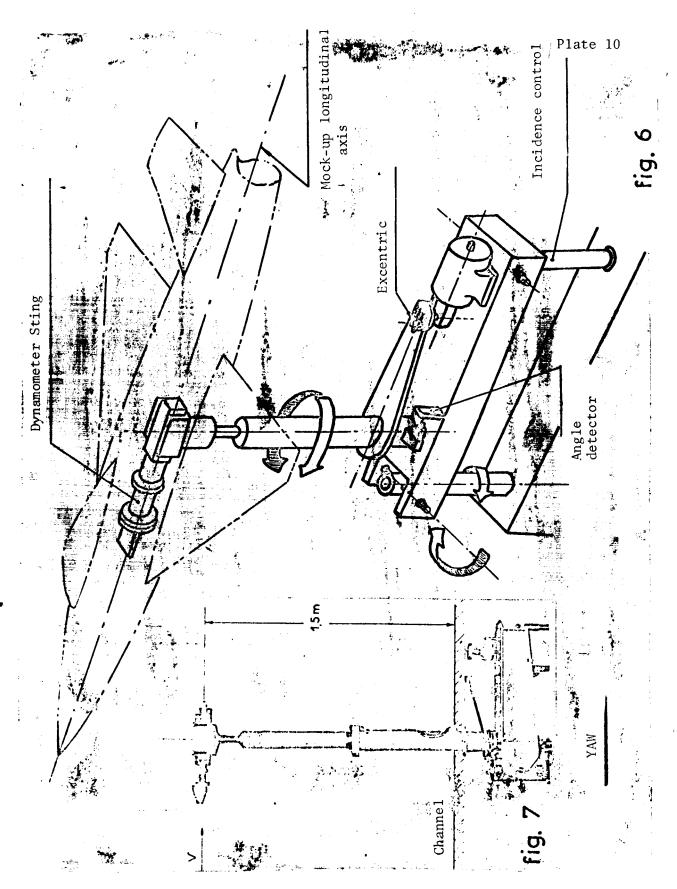
 $\label{eq:roll_power_roll} \textbf{ROLL DYNAMOMETER}$  Comparison in sensitivity and flexibility

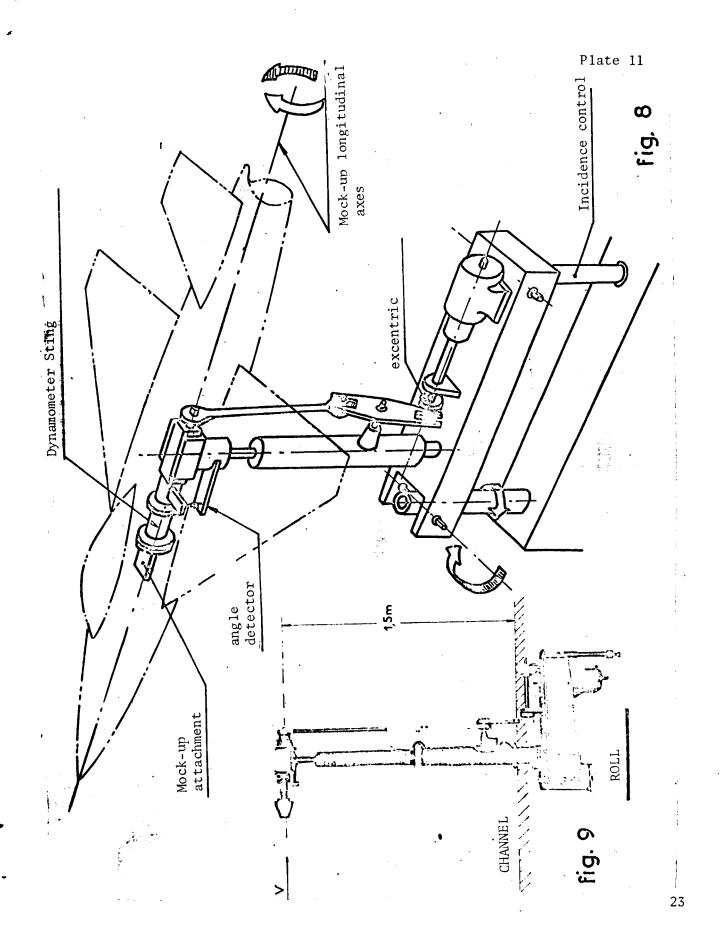


Strain detector	Semi-conductor	Resistance	ance wire		
Section	3 -9 -	9	-9-  -9- 		
Roll response in $10^{-6} \Delta R/R$ for L = 9.81 m.N	180,000	3,000	25,000		
Interactions $\begin{cases} M \\ N \\ \end{cases}$ due to $\begin{cases} R \\ R \\ \end{cases}$	3% 1% 0.1% 0.4%	None unmeasured	<0.1%		
Flexibility $\Delta \Phi/_{\Delta L}$ in r/mN	0.0031	0.0031	0.016		









THE CHALAIS-MEUDON S<sub>1</sub> AND S<sub>2</sub> BALANCE.

THE CHALAIS-MEUDON S <sub>1</sub> AND S	2 BALANCE.
Amplitudes $\Theta$ , $\Psi_1$ , $\Phi_1$ .	± 1 à ± 3 degrees
Mean incidence	0 ≤ i ≤ 30 degrees
Mean side-slip	.12 & i & 12 degrees
Frequency	1 ≤ f ≤ 2 Hz
5-component moment	$(M_1^1, N_2^1)$ leading
dynamometer	$L_{1}^{\alpha}\begin{cases}M_{1}^{1} & N_{1}^{1} & \text{leading}\\M_{1}^{2} & N_{1}^{2} & \text{trailing}\end{cases}$
Distance between leading and trailing axes	
	6.3 mm
Maximum amplitudes of moments	± 100 Nm
Measurement threshold	0,04 Nm
Maximum mock-up mass	60 Kg
Size of balance head	<pre>     cylinder</pre>

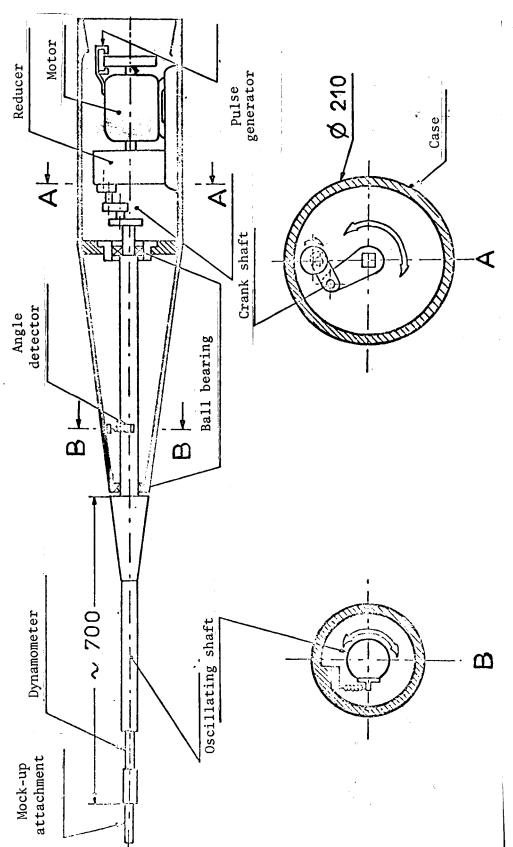
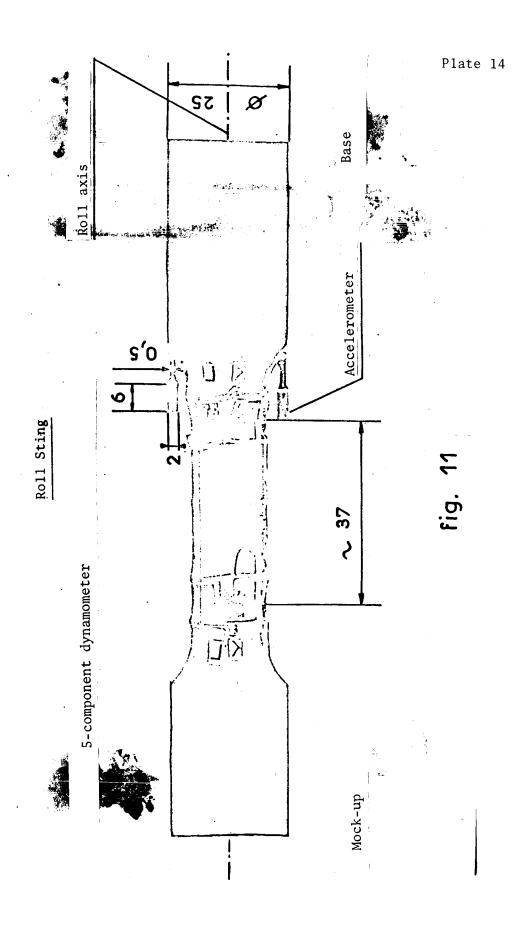


Figure 10. S2 Modane Roll Balance



### MODAN S<sub>2</sub> ROLL BALANCE.

Roll angle amplitude  $\Phi$ 

±3 degrees

Frequency

 $5 \le f \le 10 \text{ Hz}$ 

5-component moment dynamometer

 $L_1 \in \begin{cases} M_1^1 & N_1^2 \text{ leading} \\ M_1^2 & N_1^2 \text{ trailing} \end{cases}$ 

Distance between leading and trailing axes

34 mm

Maximum amplitude of moments

30 Nm

Measurement threshold

0.01 Nm

Transverse accelerometer; measurement threshold

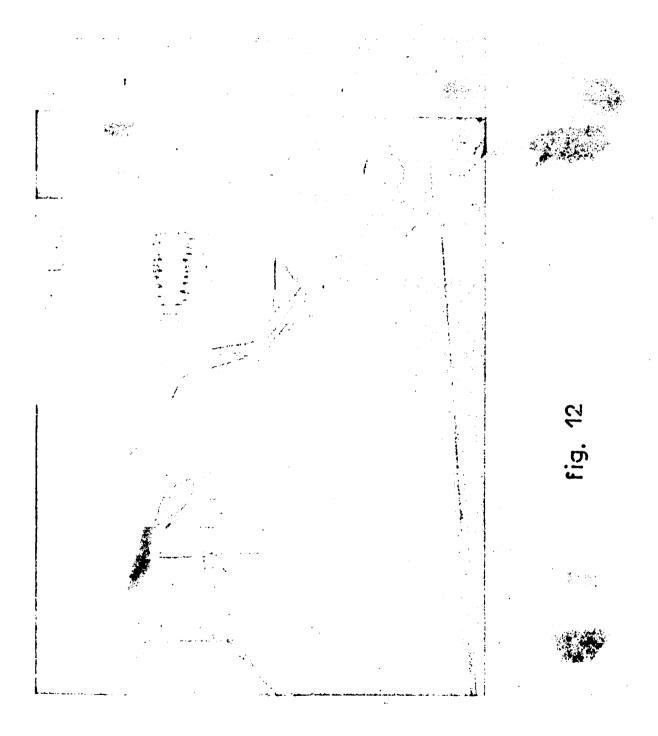
0.0025 g

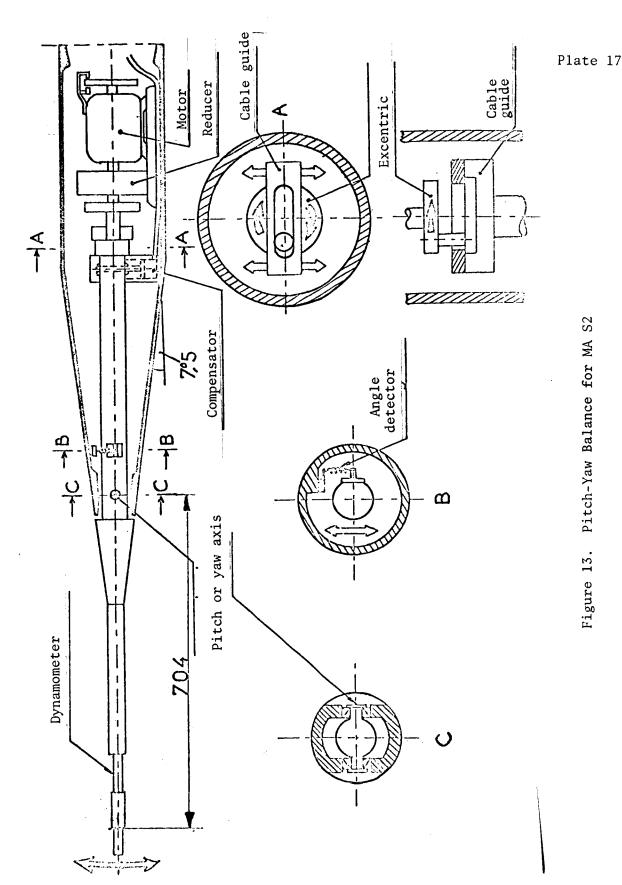
Dimensions of cylinder wall for dynamometer sting

 $\begin{cases} \text{diameter 25 cm} \\ \text{length} & 60 \text{ cm} \end{cases}$ 

Mock-up mass

6 Kg





Pitch-Yaw Balance for MA S2 Figure 13.

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BREGUET 941

#### Landing Configuration

### 1) Comparison of results from flight and analogue computer

	SYMBOL	FLIGHT	COMPUT (1)	ER (2)
Dutch roll	time in seconds	ì	7.4	8.7
Responses to one step on rudder				
Angular velocity of maximum yaw	r <sub>1</sub> (rs <sup>-1</sup> ) p <sub>1</sub> ( ") j dg	-0.16	-0.2	-0.17
Angular velocity of maximum roll	p <sub>1</sub> (")	-0.09	-0.1	-0.12
Side-slip angle	j dg	27.5°	25°	25°
Response to one step on ailerons				
Angular velocity of maximum roll	p <sub>1</sub> (rs <sup>-1</sup> )	0.4	0.45	0.41

#### 2) Comparison of computer and wind-tunnel

Coefficients		Clp <sub>1</sub>	$Cnr_1$	$Cnp_1$	Clr <sub>1</sub>	Clj <sub>1</sub>	Cnj <sub>1</sub>	Gyration r	adii (m)
								r <sub>xx</sub>	zz
Analogue	$\int_{1}^{1}$	-8.5	-8	0	6	0.6	-1.5	4	5.2
computer	<b>L</b> 2	-10	-15	-2.4	2	0.5	-1.6	4.2	5.9
Wind-tunnel		-11.5	-12	-1.2	10	1	-1.5		

